

COMPRESSED VECTOR-BASED SPECTRAL ANALYSIS METHOD AND SYSTEM
FOR MONLINEAR RF BLOCKS

CROSS-REFERENCE TO RELATED APPLICATION

This application claims the benefit of the filing date of U.S. Provisional Application No. 60/428,432, filed November 21, 2002, entitled "Compressed Vector-Based Spectral Analysis Method and System for NonLinear RF Blocks", the disclosure of which is incorporated by reference herein.

BACKGROUND OF THE INVENTION

The present invention relates generally to simulation of signal processing systems, and more particularly to simulation of RF signal processing systems.

Wireless communication circuits and systems are becoming increasingly common. Wireless communication circuits and systems are often tested by simulation before fabrication to ensure correctness of operation and to help categorize wireless device components. Simulation of wireless communication components allows designers to investigate new designs and to test design changes without expending time and money in producing physical samples.

Non-linear blocks are often present in wireless communication systems. For example, low noise amplifiers (LNAs) are often limited by voltage sources having upper and lower bounds which limit the dynamic range of the LNA. Mixers are often subject to leakage from local oscillators, with self-mixing potentially occurring with the RF signal. In addition, both active and passive devices of all blocks may introduce non-linearities at the device level.

Non-linearities may introduce additional spectral components in the form of undesired harmonics of input signals, intermodulation, and gain compression, for example. The undesired harmonics may negatively affect circuit operation. Intermodulation, particularly of undesired harmonics in a multi-tone system, may distort a signal being processed, as well increase system complexity by requiring DC offset cancellation circuitry or complex filters. Non-linearities also may result in reduced gain, through clipping or other effects.

Accordingly, preferably simulation of wireless communication systems and components includes simulation of non-linear blocks or elements. However, simulation of non-linear elements may be difficult. Simulation of non-linearities may be extremely expensive from a computational perspective, with for example extraneous signal components spread about the continuous spectrum. This computational expense is further increased if the non-linear blocks include memory.

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SUMMARY OF THE INVENTION

5 The invention provides a simulation system and method for simulating RF systems including non-linear elements.

One aspect of the invention provides a method of simulating radio frequency signal processing circuitry, comprising forming a compressed vector based equivalent of a signal; performing processing on the compressed vector based equivalent to simulate radio frequency circuitry operation, the processing forming a processed compressed vector based
10 equivalent of the signal; and forming an output signal using the processed compressed vector based equivalent of the signal.

Another aspect of the invention provides a method of modelling circuitry, comprising converting first signals to compressed equivalent signals; processing the compressed equivalent signals to form further compressed equivalent signals; and converting the further
15 compressed equivalent signals to second signals.

Another aspect of the invention provides a system for performing RF signal processing modelling, the system comprising signal generator blocks forming compressed vector based equivalent signal representations; RF signal processing blocks processing compressed vector based equivalent signal representations; and conversion blocks converting
20 compressed vector based equivalent signals to RF signal representations.

These and other aspects of the invention are more fully understood in view of this disclosure.

BRIEF DESCRIPTION OF THE FIGURES

25 FIG. 1 illustrates an example RF signal;

FIG. 2 illustrates the example RF signal with bands of the example RF signal translated to an orthogonal plane;

FIG. 3 is a block diagram of a system in accordance with aspects of the invention;

FIG. 4 is a flow diagram of a process in accordance with aspects of the invention;

30 FIG. 5 is a further block diagram of a system in accordance with aspects of the invention;

FIG. 6 is a block diagram of a system simulated in accordance with aspects of the invention;

FIG. 7 is a graph of power spectral density (PSD) of an interference signal;

35 FIG. 8 is a graph of a simulated output of a linear LNA in the system of FIG. 6;

FIG. 9 is a graph of a simulated output of a linear mixer in the system of FIG. 6;

FIG. 10 is a block diagram of a mixer simulated in accordance with aspects of the invention;

FIG. 11 is a graph of a simulated output of a non-linear LNA of the system of FIG. 6;

FIG. 12 is a graph of a simulated output of a non-linear mixer of the system of FIG. 6;

and

FIG. 13 is a block diagram of a CVB time domain implementation of a function.

DETAILED DESCRIPTION

FIG. 1 illustrates an example RF signal. The example RF signal components centered about frequencies f_0 , f_1 , f_2 and f_3 . The signal components are non-zero in frequency bands having bandwidths B_0 , B_1 , B_2 , and B_3 , each centered about f_0 , f_1 , f_2 , and f_3 , respectively. As illustrated, elsewhere in the frequency spectrum the RF signal is zero. In actuality, noise and various other factors may result in non-zero signal components outside of the frequency bands but these signal components are often of relatively low strength.

The RF signal may be viewed as similar to RF signals often encountered in wireless communication systems. For example, a wireless communication system may utilize a carrier frequency, represented in FIG. 1 as f_1 . Harmonics of the signal at the carrier frequency are found at frequencies f_2 and f_3 . A subharmonic, or a DC component, is located at frequency f_0 . Often, only the signal components about the carrier frequency and a few of the harmonics are of sufficient strength to be of interest. Thus, for the RF signal of FIG. 1, the signal components centered about f_0 , f_1 , f_2 , and f_3 may be considered frequency bands of interest.

Accordingly, aspects of the invention may be viewed as using only frequency bands of interest in simulation of a device, or of non-linear blocks of a device. In FIG. 2 the signal components in the frequency bands of interest of FIG. 1 are orthogonally transformed to lower frequencies. This is accomplished by defining orthogonal coordinates in an orthogonal plane. The signal components in the frequency bands of interest are translated to the orthogonal plane. If the signal components are viewed as vectors, the signal components in the orthogonal plane may be viewed as compressed vectors, as the vector information in the orthogonal plane is reduced compared to the vector information in the frequency plane.

As an example, consider a 900 GSM 900 MHz application. The application has a carrier frequency of 900 MHz. In the example, the application has a third order non-linearity, so that three harmonics are of interest. The total signal bandwidth is therefore 2.7 GHz. If a sampling frequency is 1 KHz, a vector of length 2,7000,000 defines the sampled signal. If, however, the channel bandwidth is 6 MHz a significant portion of the vector contains information not of particular importance.

Creation of vectors containing information for frequency bands of interest, for example in a matrix form, allows for significantly reduced, or compressed, vector size. As the three harmonics are of interest in the example, four vectors may be formed, each defined by samples formed using a 1 KHz sampling frequency in the frequency bands of interest. Each band provides a vector of length 6,000, and the four frequency bands of interest therefore provide a matrix with 24,000 entries, as opposed to 2,700,000 entries otherwise provided. A reduced number of computations may be performed in view of the reduced matrix size.

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In aspects of the invention, summation, multiplication, and convolution operations are also modified so as to provide operations for the translated signal components that are substantially equivalent to those operations for untranslated signals. In aspects of the invention, these operations are defined as follows.

A discrete signal $x[n]$ is a Piecewise Non-Zero (PWNZ) signal if it can be described as follows:

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$$x[n] = \begin{cases} x_i[n] & N_{il} \leq n \leq N_{ih} \\ 0 & \text{E.W} \end{cases}$$

$$1 \leq i \leq M < \infty$$

$$n \in Z$$

$$N_{il} \leq N_{ih} < \infty$$

$$N_{il}, N_{ih} \in Z$$
(1)

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A discrete signal $x[n]$ is a Equally Piecewise Non-Zero (EPWNZ) signal if it is PWNZ with the following properties:

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$$N_{ih} - N_{il} + 1 = L_p$$

$$\forall i \in [1, M]$$

where L_p is the piece length

(2)

Using the compressed vector terminology of above, a compressed vector-based (CVB) equivalent of an EPWNZ signal is:

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$$x_{vp}[n] = \begin{bmatrix} x_1[n] \\ \dots \\ x_M[n] \end{bmatrix} \quad \text{or} \quad x_{vp} = \begin{bmatrix} x_1 \\ \dots \\ x_M \end{bmatrix}$$
(3)

Where $x_i \in R^{1 \times L_p}$ and $x_{vp} \in R^{M \times L_p}$

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Summation of CVB equivalent signals may be considered as:

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Given $z_{vp}[n]$ as the summation of $x_{vp}[n]$ and $y_{vp}[n]$ (i.e. $z_{vp}[n] = x_{vp}[n] +_{vp} y_{vp}[n]$ where “ $+_{vp}$ ” is a symbol of summation of two CVB equivalent signals), then

$$z_{VP}[n] = x_{VP}[n] +_{VP} y_{VP}[n]$$

$$z_{VP}[n] = \begin{bmatrix} z_1[n] \\ \dots \\ z_M[n] \end{bmatrix} = \begin{bmatrix} x_1[n] + y_1[n] \\ \dots \\ x_M[n] + y_M[n] \end{bmatrix} \quad (4)$$

Where x_i, y_i , and $z_i \in R^{1 \times L_p}$ and x_{VP}, y_{VP} , and $z_{VP} \in R^{M \times L_p}$. Also "+" is the componentwise summation of two $1 \times L_p$ vectors.

Subtraction of CVB equivalent signals may be considered as:

Given $z_{VP}[n]$ as the subtraction of $x_{VP}[n]$ and $y_{VP}[n]$ (i.e. $z_{VP}[n] = x_{VP}[n] -_{VP} y_{VP}[n]$ where $-_{VP}$ is a symbol of subtraction of two CVB equivalent signals), then

$$z_{VP}[n] = x_{VP}[n] -_{VP} y_{VP}[n]$$

$$z_{VP}[n] = \begin{bmatrix} z_1[n] \\ \dots \\ z_M[n] \end{bmatrix} = \begin{bmatrix} x_1[n] - y_1[n] \\ \dots \\ x_M[n] - y_M[n] \end{bmatrix} \quad (5)$$

Where x_i, y_i , and $z_i \in R^{1 \times L_p}$ and x_{VP}, y_{VP} , and $z_{VP} \in R^{M \times L_p}$. Also "-" is the componentwise subtraction of two $1 \times L_p$ vectors.

Multiplication of CVB equivalent signals may be considered as:

Given $z_{VP}[n]$ as the multiplication of $x_{VP}[n]$ and $y_{VP}[n]$ (i.e. $z_{VP}[n] = x_{VP}[n] \times_{VP} y_{VP}[n]$ where " \times_{VP} " is a symbol of multiplication of two CVB equivalent signals), then

$$z_{VP}[n] = x_{VP}[n] \times_{VP} y_{VP}[n]$$

$$z_{VP}[n] = \begin{bmatrix} z_1[n] \\ \dots \\ z_M[n] \end{bmatrix} = \begin{bmatrix} x_1[n] \times y_1[n] \\ \dots \\ x_M[n] \times y_M[n] \end{bmatrix} \quad (6)$$

Where x_i, y_i , and $z_i \in R^{1 \times L_p}$ and x_{VP}, y_{VP} , and $z_{VP} \in R^{M \times L_p}$. Also " \times " is the componentwise multiplication of two $1 \times L_p$ vectors.

Division of CVB equivalent signals may be considered as:

Given $z_{vp}[n]$ as the division of $x_{vp}[n]$ and $y_{vp}[n]$ (i.e. $z_{vp}[n] = x_{vp}[n] \div_{vp} y_{vp}[n]$ where " \div_{vp} " is a symbol of division of two CVB equivalent signals), then

$$z_{vp}[n] = x_{vp}[n] \underset{vp}{\div} y_{vp}[n]$$

$$z_{vp}[n] = \begin{bmatrix} z_1[n] \\ \dots \\ z_M[n] \end{bmatrix} = \begin{bmatrix} x_1[n] \div y_1[n] \\ \dots \\ x_M[n] \div y_M[n] \end{bmatrix} \quad (7)$$

Where x_i, y_i , and $z_i \in R^{1 \times L_p}$ and x_{vp}, y_{vp} , and $z_{vp} \in R^{M \times L_p}$. Also " \div " is the componentwise division of two $1 \times L_p$ vectors.

Scalar multiplication of a CVB equivalent signal may be considered as:

Given $z_{vp}[n]$ as the scalar multiplication of $x_{vp}[n]$ with the scalar α (i.e. $z_{vp}[n] = \alpha \cdot_{vp} x_{vp}[n]$ where " \cdot_{vp} " is a symbol of a scalar multiplication of a CVB equivalent signal with a scalar), then

$$z_{vp}[n] = \alpha \cdot_{vp} x_{vp}[n]$$

$$z_{vp}[n] = \begin{bmatrix} z_1[n] \\ \dots \\ z_M[n] \end{bmatrix} = \begin{bmatrix} \alpha x_1[n] \\ \dots \\ \alpha x_M[n] \end{bmatrix} \quad (8)$$

Where x_i , and $z_i \in R^{1 \times L_p}$ and x_{vp} , and $z_{vp} \in R^{M \times L_p}$. Also " αx_i " is the componentwise scalar multiplication of a $1 \times L_p$ vector and a scalar.

Convolution of CVB equivalent signals may be considered as:

Given $z_{vp}[n]$ as the convolution of $x_{vp}[n]$ and $y_{vp}[n]$ (i.e. $z_{vp}[n] = x_{vp}[n] \underset{vp}{\otimes} y_{vp}[n]$ where " $\underset{vp}{\otimes}$ " then

$$\begin{aligned}
 z_i = & \begin{cases} \sum_{k=1}^{M-i} y_{(M+2-i-k)} \otimes x_{(M+1-k)} + \sum_{k=1}^i y_{Fk} \otimes x_{F(i+1-k)} + \sum_{k=i+1}^{M-1} y_{Fk} \otimes x_{F(k-i+1)} \\ \quad + y_{F(M)} \otimes x_{(M+1-i)} & i \in [1, M-2] \\ \\ \sum_{k=1}^{M-i} y_{(M+2-i-k)} \otimes x_{(M+1-k)} + \sum_{k=1}^i y_{Fk} \otimes x_{F(i+1-k)} \\ \quad + y_{F(M)} \otimes x_{(M+1-i)} & i = M-1 \\ \\ \sum_{k=1}^{2M-i-1} y_{F(k+i-M)} \otimes x_{(M-k+1)} + y_{F(M)} \otimes x_{(i-M+1)} & i \in [M, 2M-2] \\ \\ y_{F(M)} \otimes x_{(i-M+1)} & i = 2M-1 \end{cases} \quad (9)
 \end{aligned}$$

In which x_{Fi} and y_{Fi} are flipped version of x_i and y_i respectively (i.e. $x_{Fi}(n) = x_i(\text{length}(x_i) - n)$). M is the maximum number of sub-pieces taken into account, and \otimes is as follows:

$$x_i \otimes y_j = \int_{-\infty}^{\infty} x_i(F) y_j(F-f) dF \quad (10)$$

In some aspects of the invention, $x_i \otimes y_j$ is substituted with a regular convolution if $y_j(F-f) = y_j(f-F)$.

FIG. 3 is a block diagram of a simulation system using frequency bands of interest, in some aspects in terms of compressed vectors as discussed above. In the block diagram of FIG. 3, an input signal 301 (or signals) is provided to a converter 303. The converter converts the input signal to a CVB signal. The conversion in some embodiments makes use of appropriate approximation functions such as a sinc function or other functions. The converter provides the CVB signal to a CVB processing block 305, which performs various operations as described on the input signal and signals generated internal to the CVB processing block. The signals generated internal to the CVB processing block may be formed by internal signal generation blocks, by processing the input signal, by various combinations of the two, or signals ultimately generated from a combination of some or all of these signals. The CVB processing block provides resulting signals to a reversion block 307. The reversion block converts the signals back to the form of the input signals, either time domain signals or frequency domain signals as the case may be. If appropriate, Fast Fourier Transform (FFT) and inverse FFT (iFFT) processing may be used. The reversion block provides an output signal 309 (or signals).

In various aspects of the invention the CVB signals are in terms of dB, while in other

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aspects of the invention other scales are used.

FIG. 4 is a flow diagram of a process of simulating a component or system using frequency bands of interest. In Block 401 an input signal (or signals) is converted to a CVB format. In block 403 the system is simulated using CVB operations, for example as described above, and CVB format results are produced. In block 405 the CVB format results are reconverted to the form of the input signal and provided as an output.

FIG. 5 is a block diagram of a CVB processing block. The CVB processing block receives an input signal 501 in CVB format. The input signal is provided to a first simulation block 503. The first simulation block performs operations as described above and below. The CVB processing block also includes a first signal generator block 505 and a second signal generator block 507. In some embodiments, the signal generator blocks are white Gaussian noise generators, adjustable single tone generators, adjustable two tone generators, adjustable mult-tone generators, GSM900 standard power spectral density (PSD) mask generators, GSM900 adjustable PSD mask generators, GSM standard Interferer generators, GSM adjustable Interferer generators, or adjustable white Gaussian noise generators or oscillators. The signal generation blocks may be developed using the operations described above and below.

In the CVB processing block of FIG. 5 the first signal generator block provides a signal to a second simulation block 509. The second signal generator provides a signal to the first simulation block and the second simulation block. The first simulation block performs operations as described above and below using its input signals. Similarly, the second simulation block performs operations as described above and below using its input signals. The first simulation block and the second simulation block each provide a signal, formed by the performing of operations, to a third simulation block 511. The third simulation block performs operations as described above and below using its input signals. The third simulation block provides an output signal, formed by the performing of operations.

In various embodiments the simulation blocks may be considered as combinations of the operations described above. For example, the simulation blocks may be Linear Time Invariant without memory (LTI) blocks, Linear Time Invariant with memory (LTIM) blocks, Non-Linear Time Invariant without memory (NLTI) blocks, and Non-Linear Time Invariant with memory (NLTIM) blocks. These blocks may in turn be used to form low noise amplifier blocks, mixer blocks, and other blocks.

As a notation convenience, an input to a block may be considered to be $x(t)$ and an output of a block may be considered $y(t)$. Also as a notation convenience $X(f)$ and $Y(f)$ may be considered Fourier transforms of $x(t)$ and $y(t)$, respectively.

For an LTI operation $y(t)=\alpha_1 x(t)$ and $Y(f)=\alpha_1 X(f)$, where α_1 is a constant scalar. The CVB equivalent representation of the LTI operation, the LTI block, in the frequency domain is $Y_{vp}(f)=\alpha_{1 \cdot vp} X_{vp}(f)$.

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For an LTIM operation $y(t) = \int_{-\infty}^{\infty} h(\tau)x(t-\tau)d\tau$ and $Y(f)=H(f)X(f)$, where $H(f)$ is the

5 Fourier transform of the impulse response $h(\tau)$.

The CVB equivalent representation of the LTIM operation, the LTIM block, in the frequency domain is $Y_{vp}(f) = H_{vp}(f) \underset{vp}{\times} X_{vp}(f)$, where $H_{vp}(f)$ is the CVB equivalent of $H(f)$.

For an NLTI operation,

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$$y(t) = \alpha_0 + \alpha_1 x(t) + \alpha_2 x^2(t) + \alpha_3 x^3(t) + \dots$$

$$Y(f) = \alpha_0 \delta(f) + \alpha_1 X(f) + \alpha_2 X(f) * X(f) + \alpha_3 X(f) * X(f) * X(f) + \dots$$

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Where $\alpha_1, \alpha_2, \dots$ are coefficients representing non-linearity of a device and $*$ indicates convolution of two signals. The coefficients may be extracted, for example, by performing curve fitting on a curve relating inputs and outputs of the device. The CVB equivalent representation of the NLTI operation, the NLTI block, in the frequency domain is

$$Y_{vp}(f) = \alpha_0 + \alpha_1 \underset{vp}{\cdot} X_{vp}(f) + \alpha_2 \underset{vp}{\cdot} X_{vp}(f) \underset{vp}{\otimes} X_{vp}(f) + \alpha_3 \underset{vp}{\cdot} X_{vp}(f) \underset{vp}{\otimes} X_{vp}(f) \underset{vp}{\otimes} X_{vp}(f) + \dots$$

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In some embodiments NLTIM blocks are modeled as combinations of NLTI sub-blocks and LTIM sub-blocks. In other embodiments a Volterra series method is used. In a Volterra series an n^{th} order non-linear operator is described as

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$$y(t) = \int_{-\infty}^{\infty} h_1(\tau_1)x(t-\tau_1)d\tau_1 + \dots + \int_{-\infty}^{\infty} \dots \int_{-\infty}^{\infty} h_n(\tau_1, \dots, \tau_n)x(t-\tau_1)\dots x(t-\tau_n)d\tau_1 \dots d\tau_n$$

in which $x(t)$ is the input, $y(t)$ is the output, and $h_n(\tau_1, \dots, \tau_n) = 0$ for any $\tau_j < 0$ $j = 1, \dots, n$.

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Further information may be found in Schetzen, M., "The Volterra and Wiener Theories of Nonlinear Systems" (1980), the disclosure of which is incorporated by reference.

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Simulation may be computationally expensive when convolution operations are performed in the frequency domain. Accordingly, in some embodiments of the invention CVB equivalent signals in the time domain are used, allowing for, for example, multiplication in the time domain instead of convolution in the frequency domain. A real time domain signal $s(t)$ has a Fourier transform $S(f)$. $S_{vb}(f)$ is a CVB equivalent representation in the frequency domain. The CVB equivalent representation in the time domain is $s_{vb}(t)$, with

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$$s_{VB}(t) = \begin{bmatrix} s_{VB0}(t) \\ s_{VB1}(t) \\ \dots \\ s_{VBM}(t) \end{bmatrix}$$

and

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$$s_{VBk}(t) = [s(t) \cdot \exp(-j2\pi f_c t)] * \left[\left(\frac{1}{\pi t} \right) \cdot \sin(\pi B t) \right]$$

which utilizes an approximation function, and where f_c is the carrier frequency and B is the bandwidth of interest. For the frequency domain

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$$S_{VB}(f) = \begin{bmatrix} S_{VB0}(f) \\ S_{VB1}(f) \\ \dots \\ S_{VBM}(f) \end{bmatrix}$$

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with

$$S_{VBk}(f) = F\{s_{VBk}(t)\}$$

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CVB equivalent systems are formed using a combination of frequency shift blocks and samplings. For example $f(x)=x^2$,

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$$f_{VB}(x_{VB}) = \begin{bmatrix} f_{VB0}(x_{VB}) \\ f_{VB1}(x_{VB}) \\ \dots \\ f_{VBM}(x_{VB}) \end{bmatrix}$$

may be implemented as shown in FIG. 13, with a sampling frequency greater than the signal bandwidth.

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FIG. 6 is a block diagram of a simplified RF receiver front-end. The front-end includes an LNA 601 receiving an input signal. The LNA amplifies the input signal to provide a first input to a mixer 603. The mixer receives as a second input the output of a local oscillator (LO) 605. The mixer mixes the two signals to form an output signal.

As an example, the input signal is a GSM900 standard Interference signal. FIG. 7 is a graph of the input signal as provided by a CVB signal generation block. FIG. 8 is a graph of an output of the LNA when the LNA is provided the input signal of FIG. 7 and the LNA is

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modeled as an LTI block. Similarly, FIG. 9 is a graph of an output of the mixer of FIG. 6 when the mixer is modeled as a linear mixer.

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The system of FIG. 6 may also be modeled as a non-linear system. For example, the LNA may be modeled as NLTI block. In one embodiment, the LNA is modeled as an NLTI with

$$y(t) = \alpha_0 + \alpha_1 x(t) + \alpha_2 x^2(t) + \alpha_3 x^3(t)$$

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With the non-linear coefficients derived from curve fitting, with curves generated for example using tools from Cadence corporation. In the example described the coefficients are

$$\alpha_0 = 0 \quad \alpha_1 = 1 \quad \alpha_2 = 0.27 \quad \alpha_3 = -4.5.$$

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Similarly, the mixer may be modeled as a non-linear block. In the example described, the mixer is modeled in accordance with the block diagram of FIG. 10. In FIG. 10, the mixer is an NLTI block 1001. The NLTI block receives an input from an LO 1003. In addition, with RF input to the mixer, LO to RF leakage is modeled using a gain block 1005, with LO to RF isolation being 30dB. RF to IF leakage and RF to LO leakage are assumed negligible. The mixer is modeled by

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$$y(t) = \alpha_0 + \alpha_1 x(t) + \alpha_2 x^2(t) + \alpha_3 x^3(t)$$

The coefficients are derived using curve fitting, with for example curves generated using tools from Cadence Corporation. In the described example, the coefficients are

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$$\alpha_0 = 0 \quad \alpha_1 = 1 \quad \alpha_2 = 0.32 \quad \alpha_3 = -3.21.$$

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Simulation results are shown in the graphs of FIGs. 11 and 12, with the graph of FIG. 11 showing the LNA output and the graph of FIG. 12 showing the mixer output. The simulation time, using an Intel Corporation Pentium 4 equipped personal computer with a frequency resolution of 5KHz and a 6GHz signal bandwidth, was less than one minute.

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Accordingly, the invention provides a modeling system and method using compressed vectors. Although the invention has been described in certain embodiments, it should be recognized that the invention encompasses the claims supported by this disclosure and the their equivalents.